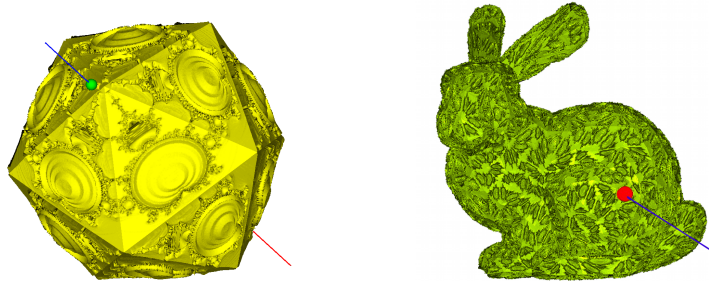


# A hybrid rugosity mesostructure (HRM) for faster rendering of fine haptic detail

Víctor Theoktisto<sup>1</sup>, Marta Fairén<sup>2</sup>, and Isabel Navazo<sup>2</sup>  
vtheok@usb.ve {mfairén, isabel}@lsi.upc.es

<sup>1</sup> Universidad Simón Bolívar, Caracas, Venezuela

<sup>2</sup> Universitat Politècnica de Catalunya, Barcelona, Spain



**Abstract.** We propose a faster method for surface haptic rendering using image-based Hybrid Rugosity Mesostructures (HRMs), paired maps with per-face heightfield displacements and normalmaps, which are layered on top of a much decimated mesh. The haptic probe’s force response algorithm is modulated using the blended HRM coat to render surface features at much lower costs. The proposed method solves typical problems at edge crossings, concave foldings and texture transitions. To prove the wellness of the approach, a usability testbed framework was built to measure and compare experimental results of haptic rendering approaches. Trial results of user testing evaluations show the goodness of the proposed HRM technique, rendering accurate 3D surface detail at high sampling rates, deriving useful modeling and perception thresholds for this technique.

*Keywords:* Haptic Rendering; Mesostructure; Displacement mapping.

## 1 Introduction

Haptic perception is the ability to touch and sense variations in geometry, roughness, texture and other volume or surface detail in computer-generated objects, necessary in fields such as nanomaterials manipulation, surgical training, virtual prototyping, machine assembly and digital sculpting. Haptic rendering of surface relief in dense models requires of special data structures, force-feedback device probes and high sampling rates for accurate model perception. Herein we describe a hybrid image-based haptic rendering approach for fast and accurate perception of surface features ranging from fine creases to major topographic features, providing a measure of performance against the existing geometric-based haptic rendering algorithms. Our main contributions are:

- (i) A specific model and algorithm for rendering image-based mesostructure surface details, mapping dual displacement and normal maps onto underlying simplified geometries (Algorithm 2);
- (ii) A blending function for smoothing height/normal computation at folding edges (section 4.1) and mesostructure transitions (section 4.2); and
- (iii) A battery of usability benchmark tests over a chosen set of meshes and mesostructures, allowing qualitative measures of feature perception at varying resolutions (section 5).

Using the previous experimental testing protocol, we achieve accurate haptic perception of fine surface detail without compromising rendering rates or fidelity of touch, with the stated objective of rendering complex detail not present in the original geometry at very low processing costs.

## 2 Related work

The term haptic rendering as defined by Zilles and Salisbury [1] denotes the real-time generation of a constraints-based force in response to users' interactions with objects, detecting collisions with a force-feedback device placed into a 3D environment. A high priority event loop checks for contacts against the geometry, after which it generates at the device new forces and torques of varying direction and magnitude [2].

A first effort to measure haptic discrimination of 2D textures was the Sandpaper System by Minsky and Lederman [3]. Users manipulated a force-feedback joystick to traverse several simple textures and report qualitative roughness differences. Siira and Pai [4] incorporated a stochastic model of physically correct surface properties to produce the appropriate textural feel, including friction and lateral forces. Costa and Cutkosky [5] generated fractal rugosity procedurally on flat surfaces and measured perception thresholds.

Using a third object as an extended probe allows real-time texture differentiation and shape perception [6]. Detecting friction among objects is achieved by rubbing simulated known material against each others [7] and the expected friction force using common physical models.

These efforts choose among several alternatives for modeling and rendering surfaces. Gregory *et al*'s H-Collide [8] use hybrid hierarchical representation of uniform grids and trees of tight-fitting oriented bounding boxes, whereas Johnson [9] uses a pure geometric render approach for arbitrary polygons using neighborhood proximities. Morgenbesser and Srinivasan in [10] proposed the method of *force shading*, akin to *Phong shading* and *bump-mapping*. The force response' vector is interpolated from nearby vertices, but it is unable to elicit accurate geometric up-down perception. A global procedure for mapping a gray-scale image as a displacement map for point-based haptic rendering is given by Ho *et al* [11]. It works only for convex objects of genus 0, without any assessment of sensation fidelity.

Inadequate modeling or suboptimal rendering produce instabilities in the force response, as shown in the work of Choi and Tan [12]. Collisions are detected against a coarse geometry and then against a second microgeometry layer. Incorrect renderings when traversing concave foldings are identified but not addressed. A similar approach for geometric sculpting with 2D textures and a haptic stylus is used by Kim *et al* [13]. Potter *et al* [14] provide a simple model to perceive haptic variation in large heightfield terrains, detecting collisions against the terrain's dataset patches.

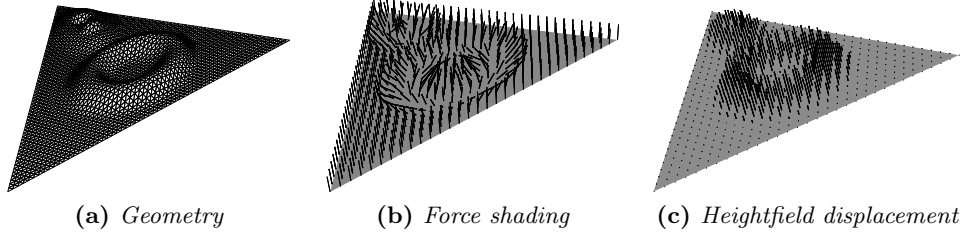
An extended survey of current haptic rendering techniques can be found in Laycock and Day [15]. From the latter review it follows that haptic rendering approaches have relied either on straightforward collisions against the mesh's triangles or a NURBS parameterization of the same. There is no formal treatment regarding the use of heightfield displacements for haptic rendering, and a lack of a unified testing framework for measuring quantitative and qualitative differences among rendering approaches in usability trials on standard models and surfaces.

## 3 Models for haptic perception of surface details

Fast algorithms for visualizing surface details of complex models using color textures and bump-mapping are well known in the literature [16]. In the case of haptic rendering, any algorithm should be efficient enough to achieve the high frequency updates (1000 Hz) required by the human sense of touch. Our objective was finding a haptic rendering algorithm for surface detail perception in triangle meshes, and compare it to other known solutions. We summarize a taxonomy for haptic detail rendering, which determines the particular algorithm to be used.

- *Geometric Detail*, rendering the surface as detailed polygonal meshes or NURBS (Figure 1a), and detecting collisions against the surfaces.
- *Surface Relief Detail*, where a haptic texture is sampled in lieu of the actual surface. Haptic textures may be based on normal force maps (Figure 1b) or heightfields (Figure 1c).

The *force shading* algorithm uses a surface normal vector field to calculate the force direction and magnitude to be applied to the haptic device when it collides with the triangle [Figure 1b]. By using this haptic rendering algorithm with its corresponding *bump-mapping* visualization, one can achieve a correct perception of surface roughness for small height differences. Collisions are always detected against the mesh triangle, but upward/downward perception from the mesh surface is not possible.



**Fig. 1:** Approaches for simulating surface details in haptic perception

We offer below a brief summary of an approach by Theoktisto *et al* [18] to render the surface detail off an underlying triangle mesh, which builds a constraint-based force response of local heightfield displacements by modulating 6 DoF spring/damper objects. The method, shown here as Algorithm 1, compares favorably against a force shading implementation for perceiving the same models, using equivalent normal force maps for texture perception.

As shown in Algorithm 1, a 3D search for a haptic collision against some small facet is substituted by a collision search against a much larger triangle, triggering the haptic rendering of the corresponding heightfield displacement map. The probe’s position is orthogonally projected onto the closest surface point of that triangle. The algorithm determines (at very low computational cost) the base triangle being *potentially* hit by the haptic probe, with ample time to sample the appropriate heightfield altitude, determine whether there is an actual penetration (the haptic probe is below that height at that point), and in that case, compute an repelling force along the triangle’s normal, proportional to the penetration difference of the haptic probe at the surface with a penalty-based force computation model. This repulsion forces the constrained proxy of the haptic probe to move towards the surface, at which point the force ceases (see figure 3). The haptic probe and the god-object are kept in sync by the constraint system.

A bounded prism or wedge is created for each mesh triangle  $T_k = \langle V_{k,0}, V_{k,1}, V_{k,2} \rangle$ , with displacements up and down a distance  $mh$  along each vertex normal, enclosing all possible heightfield values (see Figure 2). The 8 triangles thus created (2 for each of the 3 walls, plus the top and bottom lids) share the same tagging label of the base triangle, so identification of the relevant face is immediate after hitting any side of the prism.

Heightfield displacements are clamped at the edges to insure  $C^0$ -continuity. This avoids sudden height jumps at the triangles’ edge. In the case of convex folds, simple normal interpolation avoids instabilities when cruising near the edges, but this is inadequate when sizable height differences exist across face boundaries, and totally wrong for holes and concave folds.

## 4 Mesostructure model for haptic rendering

We proceed now to elaborate on a method that proposes a global solution to the afore mentioned problems. Instead of applying the force in the normal direction of the base triangle  $T_k$ , a much more accurate rendering approach applies the repulsing force in the exact direction of the normal at the specific impacted surface point. Normals are generated directly from the heightfield displacement texture and both stored as textures, creating what we call a Hybrid Rugosity Mesostructure or *HRM*. Taking into account the traversal direction when touching a surface, the haptic point is pushed in the direction of the normal, and a constraint system combines this repulsion with the force exerted by the user at the probe, producing a change of position and orientation without incurring in lagged responses.

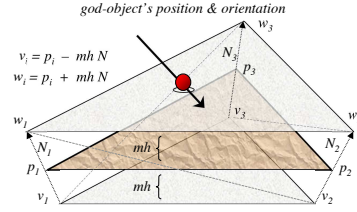
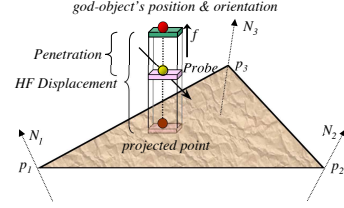
This allows to vary surface sensation exploration by “coating” a mesh with several surface reliefs at different frequencies. This image-based general procedure, shown in Algorithm 2, uses the previously defined prisms with an added twist. The HRM tuples for normal maps and heightfield displacements  $[\vec{N}(s,t), H(s,t)]$  correspond to an  $\text{RGB}\alpha$  texture, having coordinates  $\langle r, g, b, \alpha \rangle = \langle N_x, N_y, N_z, H_w \rangle$ . The

**Algorithm 1** Heightfield-displacement rendering

```

1: {Optimal probe sampling speed between 200-1000 Hz}
2: loop
3:   Sample haptic probe position  $P_H = (x_H, y_H, z_H)$ ;
4:   Detect potential collision with a triangle in the mesh;
5:   if ( $\exists$  collision with some triangle prism  $T$ ) then
6:     {haptic probe  $P_H$  is inside  $T$ 's prism}
7:     Project  $P_H$  against  $T$  obtaining surface point  $P$ ;
8:     Compute 2D texture coords  $(s, t)$  of  $P$  over  $T$ ;
9:     Sample the heightfield displacement  $Z = H(s, t)$ ;
10:    if ( $penetration = Z - distance(P_H, P) > 0$ ) then
11:      {Positive penetration, a real collision}
12:      Calculate force  $F(penetration)$ ;
13:      Apply  $F$  in the normal  $\vec{N}$  of  $T$  at the device;
14:    end if
15:  end if
16: end loop

```

**Fig. 2:** Triangle prism collision area**Fig. 3:** Collision point computation

heightfield-normal tuples may be provided as static or procedural 2D, 3D or 4D (3 + time) textures, allowing for even greater complexity of haptic perception and correspondence with visual renderers. Friction, viscosity, magnetism, color and other surface properties may be easily added as additional entries on the HRM structure, requiring only the modification of the force-response accordingly. Haptic resolution gets scaled in sync with the current visual zoom state, so features not measurable at lower zoom levels (“blurred”) become noticeable at close range, and surface perception becomes more accurate.

#### 4.1 Blending haptic mesostructure at the edges

Algorithm 2 also computes soft transitions at triangle edges having different mesostructures using a simple interpolation scheme. For each face in the mesh, we keep track of neighborhood information of all adjoining face indices. When following along the surface of the mesh, the mesostructures in neighboring faces may produce an abrupt topographic change at the edge, that if left to stand will produce a sudden force kick (in magnitude and orientation) in the haptic device. To eliminate these abrupt jumps, we follow the following stitching procedure to blend the transition among convex faces.

Heightfield and normals closer to the edges are sampled from the rugosity mesostructure using a multi-texturing approach. In Figure 4 we see a schematic of this heightfield stitching. A parametric band of size  $\rho$  extends at both sides of each edge. In this area we use an alpha-blending function. We extend each parametric distance of the triangle’s barycentric coordinates in this quantity  $\rho$ , say 0.05 (or 5%) over each HRM. Each blending map of Figure 5 is then used to compute an averaged mesostructure that spans parametrically a  $\rho$  distance across each edge.

If the projected point of the haptic probe is inside the  $\rho$  band of triangle A (in Figure 4), at least one of the barycentric coordinates of  $P_0$  is less than  $\rho$  at some edge. This point is remapped into the opposing triangle B, obtaining its local set of barycentric coordinates  $P_1$ . To blend both heights and normals, we solve for a  $t$  value between 0 and 1 out of  $P_0$ ,  $P_1$  and  $\rho$  for the chosen blending function, and obtain the corresponding weights  $\omega(t)$ . Several blending functions may be defined for different effects. If we desire no blending at all, a half white/half black map (Figure 5, No blend) will produce the abrupt relief transition at the edges, generating jumps at edge crossings. A linear gradation from white to black (Figure 5, Linear) or a sloping S-shaped curve (Figure 5, S-Shape) offer more stable and pleasant results. We use the  $\omega$  weights to compute an average height and normal direction. In the case of point  $P_2$ , some additional barycentric coordinate is also less than  $\rho$ , so this process is repeated for this adjacent edge. Point  $P_3$  falls outside of the  $\rho$  bands, so it is sampled only once.

### Algorithm 2 Haptic mesostructure-blended rendering

```

1: loop
2:   Sample haptic probe position  $P_H = (x_H, y_H, z_H)$ ;
3:   {Detect collisions against the triangle octree;}
4:   if ( $\exists$  collision at some triangle prism  $T$ ) then
5:     Project  $P_H$  against  $T$  to obtain surface point  $P$ ;
6:     Compute 2D texture coords  $(s, t)$  of  $P$  over  $T$ ;
7:     Obtain barycentric coords  $\alpha, \beta$ , and  $\gamma$  of  $P$  in  $T$ ;
8:     if ( $\exists \alpha, \beta$ , or  $\gamma \geq 1 - \rho$ ) then
9:       {We are within  $\rho$  distance of an edge}
10:       $AD \leftarrow 0$ ;  $\vec{AN} \leftarrow \vec{0}$ ;
11:      for all  $T$  and adjoining triangles  $f_i$  of  $T$  do
12:        Project  $P_H$  against  $f_i$  to obtain  $P_i$ ;
13:        Compute 2D texcoords  $(u_i, v_i)$  of  $P_i$  on  $f_i$ ;
14:        Sample HRM pair  $[\vec{N}_i(u_i, v_i), H_i(u_i, v_i)]$ ;
15:        Evaluate weights  $\omega_i$  from  $P, P_i$  and  $\rho$ ;
16:         $AD \leftarrow AD + \omega_i H_i(u_i, v_i)$ ;
17:         $\vec{AN} \leftarrow \vec{AN} + \omega_i \vec{N}_i(u_i, v_i)$ ;
18:      end for
19:       $AD \leftarrow AD / \sum \omega_i$ ;  $\vec{AN} \leftarrow \vec{AN} / |\vec{AN}|$ ;
20:    else {Collision against a single face}
21:      Sample HRM pair  $[\vec{N}(s, t), H(s, t)]$ ;
22:       $AD \leftarrow H(s, t)$ ;  $\vec{AN} \leftarrow \vec{N}(s, t)$ ;
23:    end if
24:    if ( $penetration = AD - |\vec{P}_H, \vec{P}| > 0$ ) then
25:      Calculate force magnitude  $F(penetration)$ ;
26:      Apply  $F$  in the normal  $\vec{AN}$  at the device;
27:    end if
28:  end if
29: end loop

```

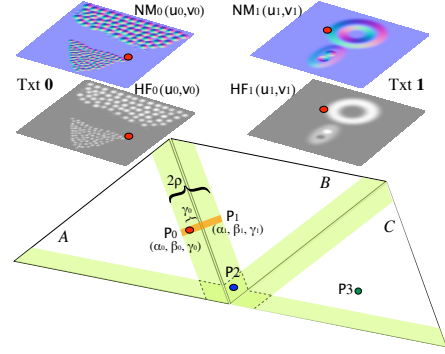


Fig. 4: HRM stitching computation

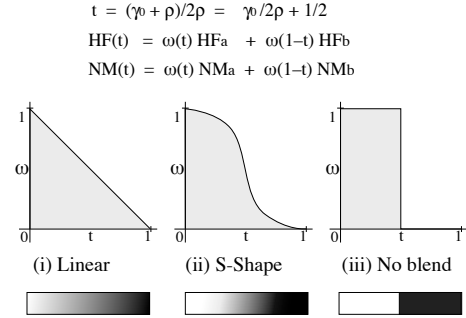


Fig. 5: Edge blending functions

## 4.2 Haptic rendering in concave faces

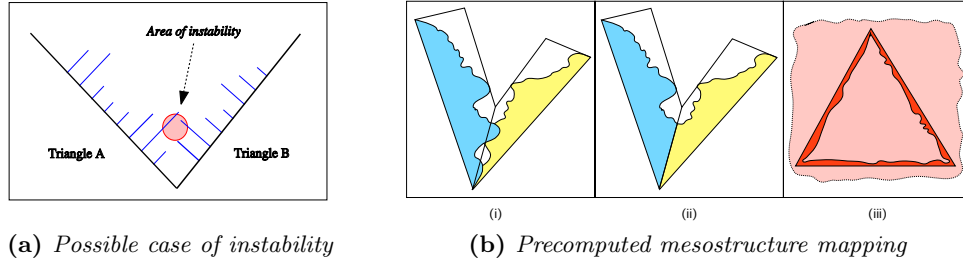
A problem mentioned before is the performance issues when rendering non-convex objects (see figure 6a). When two or more triangles form a concave fold or depression (angle between faces less than  $180^\circ$ ) the haptic probe could be inside two (or more) prisms at the same time.

Basically, the treatment of concave faces is the same applied to flat and convex faces. It will blend heights and normals in a band of size  $2\rho$  around the edges (half in one face, half on the other), so the effect will be a repulsion away from the edge. Unfortunately, this may create a back-and-forth effect at the probe (see Figure 6a), sometimes getting stuck and unable to leave the surface, or in rare cases, generating a resonance situation with ever increasing force magnitude, generating a device failure.

Our solution is to transform the initial mesostructure texture, so that height and cumulative normals are already mapped for those surface points that collide into other faces, saving the inclusion and collision tests altogether. In Figure 6b(i) we see two adjoining triangles and their corresponding unblended mesostructures (blue and yellow), with a subsurface hole (and potential device trap) laying in the middle. At Figure 6b(ii) we see the result of the blended joint mesostructure, with the hole eliminated. The probe will be pushed away in the combined correct direction.

To avoid borderline cases, we add a small  $\epsilon$  to the collided heights to avoid getting trapped in a narrow crevice or hole. The probe is detected inside the common region by a simple inclusion test, and the relevant heightfields (red) reflect the correct surface relief close to the edges (see figure 6b(iii)).

Stitching different mesostructures may be applied at triangle boundaries if so desired. When the HRMs are precomputed from existing fine geometric detail, abrupt height and normal differences are greatly minimized across edges, thus greatly reducing haptic artifacts.



**Fig. 6:** Haptic rendering in concave faces

## 5 Testing Procedure

To measure quantitatively the participants' abilities to perceive each surface's haptic properties, we devised the following testing protocol for choice meshes and textures, using both force shading and HRMs. A total of 3 separate experiments (see Table 1) were performed on the participants, plus a previous baseline perception as control setup, so users would recognize what a feature-less surface feels like.

**Table 1:** Trial tests protocol

<i>Test Description</i>	<i>Mesh</i>	<i>HRM</i>	<i>What is measuring</i>
<b>I.-</b> Quality of Visual-Haptic perception	$M_a, M_{d,j}$	$H_2, H_3, H_4$	<i>Perception differences between haptic rendering algorithms.</i>
<b>II.-</b> Perception quality of monotonous mesostructure (simple patterns).	$M_a, M_b$	$H_{1,k}$	<i>Visual-haptic resolution calibration, height variation, groove counting and orientation.</i>
<b>III.-</b> Perception quality of non-monotonous mesostructure (complex patterns).	$M_b$	$H_2, H_3, H_4, H_5, H_6, H_7$	<i>Visual-haptic correspondence, height variation, contour following, bumpy quality.</i>

**Equipment** A FCS HAPTICMaster, able to exert forces from a delicate 0.01 N up to a heavy blow of 250 N, with a built-in 3D haptic perception wedge of 40 cm x 36 cm x 1 radian. The PC is a 2.4 GHz Pentium IV with an ATI Radeon X1600 graphics card.

**Participants** Each test involved 18 different user tester/trials (6 participants, 3 trials each) for each setup. Testers were isolated and unaware of what to expect. All of them had used the haptic device before, and were instructed to maintain constant force and speed throughout each experiment. Their perception impressions were recorded from the same live questionnaire.

**Stimuli** We prepared a set of base meshes, shown on Table 2, each having some measurable perception property. To create the set of HRM coats shown on Table 3, we generated the appropriate heightfield displacement maps, and calculated their corresponding normal maps as explained in [19], (also used in force shading). In the latter manner we could dress any mesh with chosen HRM coats representing particular 3D mesostructures.

Each trial consisted in a different  $\langle Mesh, HRM, Test \rangle$  triad being executed. The experiments (shown on Table 1) were performed and measured modulating the maximum amplitude of heightfield displacements, at 1%, 5%, 10%, 15% and 20% of the average edge length of each mesh. This proved a better predictor than average triangle mesh area, since it works well even with near degenerate triangles.

### 5.1 Test I. Quality of Visual-Haptic perception

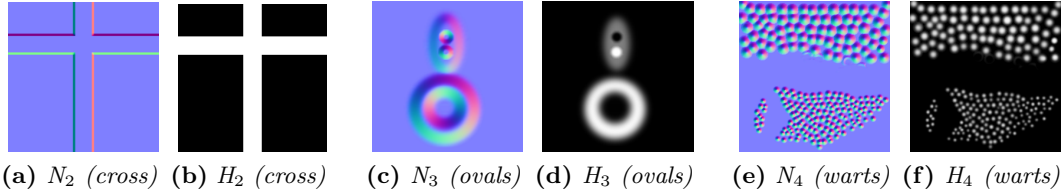
A series of spheres were built recursively at several resolutions out of a regular icosahedron, and then the synthetic HRMs shown on Figure 7 were generated. The chosen textures were: alternating polished and variable bumpy areas ( $N_4$  and  $H_4$ ), gently sloping circles within a soft gradient ( $N_3$  and  $H_3$ ), and an embossed cross having only horizontal and vertical surfaces ( $N_2$  and  $H_2$ ).

**Table 2:** Trial model meshes

Mesh	Description
$M_a$	Open regular mesh (flat triangle surface).
$M_b$	Softly convex mesh (folding angles a tad over $180^\circ$ ).
$M_c$	Convex mesh, faces folding at acute, square and obtuse angles.
$M_{d,j}$	Closed convex meshes (spheres), beginning with an Icosahedron.
$M_e$	Open concave mesh in the shape of a "cup".
$M_f$	Open mesh of a regular gradation of triangles, from big to small.
$M_g$	A much denser mesh based on $M_b$ , with very small triangles following the heightfield instead.

**Table 3:** Hybrid rugosity mesostructures

HRM	HRM feature description
$H_{1,k}, N_{1,k}$	Family of serrated textures (vertical left side; sloping right side), with peak frequency growing in $k$ .
$H_2, N_2$	Raised beams crossing at right angles.
$H_3, N_3$	Gently sloping rings, peaks and holes.
$H_4, N_4$	Bumps and warts of varying sizes and densities.
$H_5, N_5$	Raised flat cylinders (such as a coin).
$H_6, N_6$	Grooved or engraved letter $S$ (a purely negative heightfield).
$H_7, N_7$	A generated fractal landscape, with irregular peaks and valleys.

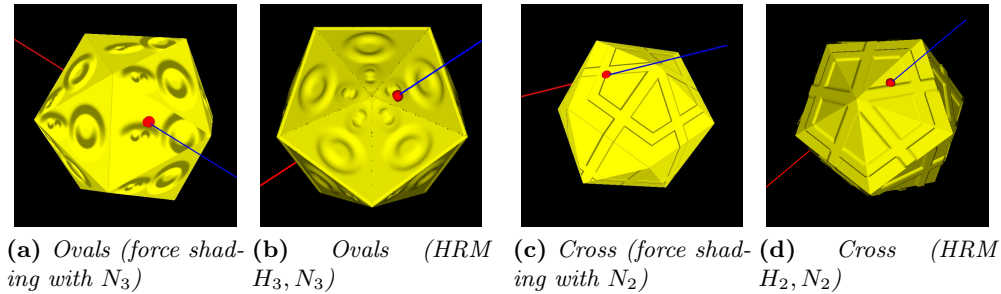


**Fig. 7:** Normals and Heights maps

**Evaluation of Results** We show on Figure 8, different renderings using force shading and HRMs. It is evident from the figures that normals in bump mapping/force shading make for a smoother visualization. However, in terms of haptic perception, the comparisons are quite different and depend on the characteristics of the texture map.

- In the case of the displacement map shown in Figure 8a, using a texture image with a big oval and two small bumps over the surface, the resulting perception is a bit different between the two methods. In the part of small bumps there is almost no difference, but in the big oval part, the force shading method only perceives the resistance for going up to the oval, while in the heightfield method the perception is clearly going up and down from it.
- In the case of the texture shown in figure 8c of a cross relief over the surface, the perception is clearly different between the two methods. In the force shading method users perceive resistance on the going up and a jump going down, but report no measurable height differences. In the HRM method the perception is more accurate, because going up and down the cross gives the feeling of a real height displacement from the base.

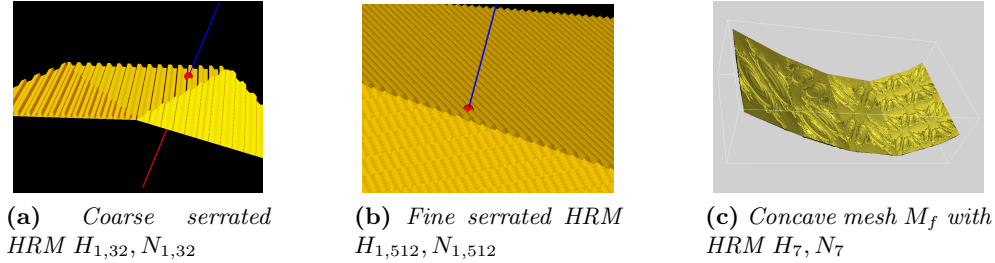
As a summary for this test, we can conclude that our HRM algorithm gives a much more accurate sense of the surface characteristics than when using force shading alone.



**Fig. 8:** Haptic perception: Force Shading vs. HRM

## 5.2 Test II. Perception of mesostructure with simple repeating patterns

This test was devised to detect the lower and upper limits of haptic modeling and perception using the HRM approach. The test measured several perception variables out of a regular serrated pattern: How does it feel when going back-and-forth? Can the ridges be counted? Are the height differences noticeable?. Each trial was performed with base mesh  $M_b$  using HRMs  $H_{1,j}$ , having regular serrated patterns at different frequencies (with corresponding normals  $N_{1,j}$ , see figures 9a and 9b). For each trial, the maximum



**Fig. 9:** Perception scaling adjustment for mesostructure

heightfield value (that is, the altitude of the prism) was modulated at 1%, 5%, 10%, 15% and 20% of the average edge length, and repeated runs with several users. Force shading failed miserably this test, detecting just unidirectional vibration at higher frequencies and shown to be unreliable at best at lower ones.

**Evaluation of results** When we tested the HRMs, ranging the surface frequencies from few ridges to many, only the last two showed a performance threshold. *Frec256* is a mesostructure that has an asymmetric serrated peak-valley combination repeated 256 times, and *Frec512* is correspondingly doubled. Results are summarized in figure 10a and figure 10b: The red (ridge count) and blue (left-to-right difference) lines in each graph represent the sample mean, and the surrounding shaded areas represent two standard deviations around the mean. Two important facts that can be extracted from this results:

- There exists a definite region for optimum perception of haptic features, having peaks and valleys of 5%-15% of a triangle’s edge size, with a “sweet spot” at altitude 10%. The 5%-15% region also holds for dynamic characteristics such as groove sense, and left-to-right or right-to-left differences. At the highest texture resolution, all test subjects felt only vibration, without any sense direction.
- Heights greater than 20% produce instabilities in the haptic device, due to fast change in surface normals, high forces in steep vertical walls, and overshoot due to feedback kick.

These results hint at a practical threshold on how well mesostructure may be modeled by this approach. In the upper end of the scale, mesh zones whose surface variation exceeds 15% of average edge size are candidates for finer remeshing. In the other end of the scale, if a triangle is perceived as too smooth, the haptic sensation may be enhanced by a coarser sampling of the same texture.

## 5.3 Test III. Perception of non-monotonous mesostructure

Here we measured the ability to perceive definite shapes in the haptic textures: A soft texture of sloping peaks and depressions; small-to-big warts; single scratches. The object of this test is the multi-modal quality of perception: how it corresponds with the visual representation and whether it can be “followed along”.

**Evaluation of results** As can be extracted from Table 4, even small scratches are felt and followed. All testers were able to accurately detect the target features even a low resolutions, except when reaching the 20% threshold level, at which point instability set in and perception degraded quickly.



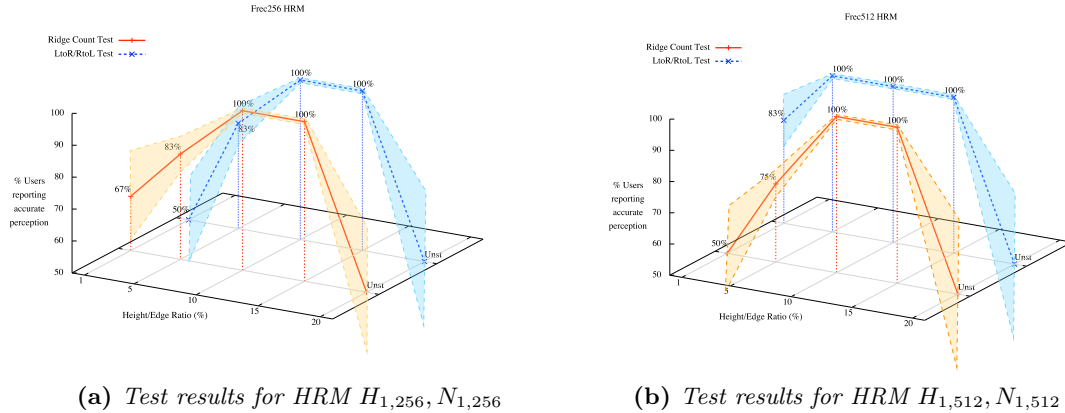


Fig. 10: Haptic perception of heightfield textures

Table 4: Haptic perception of fine features in non-monotonous mesostructure

Test	1-5%	10%	15%	20%
Round contours	yes	yes	yes	unst

Test	1-5%	10%	15%	20%
Scratches	100%	100%	100%	unst.
	yes	yes	yes	

Test	1-5%	10%	15%	20%
Small bumps	100%	100%	100%	83%
	yes	yes	yes	yes

## 6 Conclusions

We have developed a fast and accurate method for rendering local haptic texture in triangle meshes, which allows perception of correct surface details at several resolutions. This extends the use of heightfield haptics beyond the usual field of gigantic terrain textures and allows perceiving higher surface detail without modeling it geometrically. This approach can be used for locally mapping relief textures in triangular meshes and haptically render them in real time. The method even allows managing LoD in the visual and haptic resolutions for closer approximations, and we have the added benefit of having a repository of assorted HRMs, even procedural ones.

In order to apply our method for perceiving overlaid scratches on the surface [20], we have extended it to accept HRMs representing inverse heightfields. In these cases, force shading does not give the correct perception because neighboring points with converging normals actually push the haptic probe away from the scratch. Our HRM-rendering algorithm allows a correct perception and traversal along the grooves of the scratches. The approach shows ample suitability for modeling and perceiving in real time very complex surface textures of varying frequency out of simpler geometric models such as bones, major body organs, machine assembly pieces and other structures.

We are extending this research by exploring a procedure to scan the fine triangle geometry of dense meshes, and replace it with a decimated mesh of much larger triangles capturing most of the perceptible frequency details of the original triangles in a blended global HRM mesostructure atlas (height displacements, surface normals and other properties such as directed friction and stickiness).

The approach uses haptic impostors to replace the nearest object geometry, and is similar to the visualization algorithm that Policarpo [21] and Baboud [22] describe for fast shading of geometric objects using displaced-mapped impostors, either as a two-sided back/front map or a six-sided cube map.

## Acknowledgments

We thank Iban Lozano for his shader implementation, and Eva Monclús, Santiago Murillo, Antoni Xica, Joseba Rodríguez, Ramón Trueba and Marcos Balsa for their observations and patience in the testing phase. This work has been co-financed by project TIN2004-08065-C02-01 of the Spanish Government (MEC) and FEDER funding, and by project II-021-FA of the UE ALFA Cordial-2 network.

## References

1. Zilles, C., Salisbury, J.: A constraint-based god-object method for haptic display. In: Proc. IEEE Int'l Conf. Intelligent Robots and Systems, Washington, DC, USA, IEEE Computer Society (1995) 31–46
2. Martín, J., Savall, J.: Mechanisms for Haptic Torque Feedback. In: Proceedings of the First Joint Eurohaptics Conference and Symposium on Haptic Interfaces for Virtual Environment and Teleoperator Systems. (2005)
3. Minsky, M., Lederman, S.: Simulated haptic textures: Roughness. In: Proceedings of the ASME Dynamic Systems and Control Division. Volume 58. (1996)
4. Siira, J., Pai, D.K.: Haptic texturing: A stochastic approach. In: IEEE International Conference on Robotics and Automation. Volume 1. (1996)
5. Costa, M.A., Cutkosky, M.R.: Roughness perception of haptically displayed fractal surfaces. In: Proceedings of the ASME Dynamic Systems and Control Division. Volume 69. (2000)
6. Otaduy, M.A., Lin, M.C.: Stable and Responsive Six-Degree-of-Freedom Haptic Manipulation Using Implicit Integration. In: Proceedings of the First Joint Eurohaptics Conference and Symposium on Haptic Interfaces for Virtual Environment and Teleoperator Systems. (2005)
7. Richard, C., Cutkosky, M.R.: Friction Identification for Haptic Display. In: Proceedings of the 1999 ASME IMECE. (1999)
8. Gregory, A., Lin, M., Gottschalk, S., Taylor, R.: H-collide: A framework for fast and accurate collision detection for haptic interaction. In: Proceedings of IEEE Virtual Reality Conference 1999, IEEE (1999) 3845
9. Johnson, D.E., Willemsen, P.: Accelerated Haptic Rendering of Polygonal Models through Local Descent. In: Proceedings of the 12th International Symposium on Haptic Interfaces for Virtual Environment and Teleoperator Systems (HAPTICS'04). (2004)
10. Morgenbesser, H.B., Srinivasan, M.A.: Force shading for haptic shape perception. In: Proceedings of the ASME Intl Mechanical Eng. Congress and Exposition, Dynamic Systems and Control Division. (1996) 407–412
11. Ho, C.H., Basdogan, C., Srinivasan, M.A.: Efficient point-based rendering techniques for haptic display of virtual objects. *Presence* **8**(5) (October 1999) 477–491
12. Choi, S., Tan, H.Z.: Perceived instability of virtualhaptic texture. ii. effect of collision-detection algorithm. *Presence* **14**(4) (2005)
13. Kim, L., Sukhatme, G.S., Desbrun, M.: A haptic-rendering technique based on hybrid surface representation. *IEEE Computer Graphics and Applications* (March/April 2004) 66–75
14. Potter, K., Johnson, D., Cohen, E.: Height Field Haptics. In: Proceedings of the 12th International Symposium on Haptic Interfaces for Virtual Environment and Teleoperator Systems (HAPTICS'04). (2004)
15. Laycock, S.D., Day, A.M.: A survey of haptic rendering techniques. *COMPUTER GRAPHICS forum* **26**(1) (2007) 50–65
16. Blinn, J.F.: Simulation of wrinkled surfaces. In: Proceedings of SIGGRAPH'78, ACM (1978)
17. Basdogan, C., Srinivasan, M.A.: Haptic rendering in virtual environments. In Stanney, K., ed.: *Handbook of Virtual Environments*. London, Lawrence Earlbaum, Inc. (2002) 117–1343, 2212–2218
18. Theoktisto, V., Fairén, M., Navazo, I., Monclús, E.: Rendering detailed haptic textures. In: Proceedings of Second Workshop in Virtual Reality Interactions and Physical Simulations (VRIPHYS '05), Pisa, Italy. (2005)
19. Shankel, J.: Fast Heightfield Normal Calculation. In: *Game Programming Gems 3*. Charles River Media, Inc. (2002) 344–348
20. Bosch, C., Pueyo, X., Mérillau, S., Ghazanfarpour, D.: A physically-based model for rendering realistic scratches. *Computer Graphics Forum* **23**(3) (2004)
21. Policarpo, F., Oliveira, M.M., Comba, J.L.D.: Real-time relief mapping on arbitrary polygonal surfaces. In: *SI3D '05: Proceedings of the 2005 symposium on Interactive 3D graphics and games*, New York, NY, USA, ACM Press (2005) 155–162
22. Baboud, L., Décoret, X.: Rendering geometry with relief textures. In: *Graphics Interface '06*, Quebec, Canada (2006)